

## Determination of Absolute $f$ Values from Relative Intensity Measurements for Spectral Lines with Doppler Contour\*

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THE experimental determination of absolute intensities for isolated spectral lines or for entire vibration-rotation bands involves formidable experimental difficulties. For this reason it is highly desirable to consider the use of techniques which permit the determination of absolute  $f$  values from relative intensity measurements performed by the use of a low resolution spectrograph. It is the purpose of this note to call attention to a useful experimental procedure for spectral lines with Doppler contour and for optical densities which are sufficiently large to assure a nonlinear dependence of intensity on optical density. The method is a generalization of a two-path experiment proposed for emission studies on flames.<sup>1</sup>

For spectral lines with Doppler contour it is well known<sup>2</sup> that the total absorbed intensity of radiation  $A[\nu_{lu}(K)]$ , for the line identified by the index  $K$  and with center at the frequency  $\nu_{lu}$ , is

$$A[\nu_{lu}(K)] \simeq R^0(\nu_{lu}) (mc^2/2\pi kT\nu_{lu}^2)^{-1} [P_{\max}(K)X] \times \left\{ \sum_{n=0}^{\infty} \frac{[(n+1)^2(n+1)!]^{-1} [-P_{\max}(K)X]^n}{n!} \right\}, \quad (1)$$

if  $R^0(\nu_{lu})$  is the intensity of the incident radiation at  $\nu_{lu}$ ,  $m$  is the mass of the absorber,  $c$  equals the velocity of light,  $k$  is the Boltzmann constant,  $T$  represents the absolute temperature,  $X$  is the optical density (in cm-atmos) of the absorber, and  $P_{\max}$  is the maximum value of the spectral absorption coefficient (in cm<sup>-1</sup>-atmos<sup>-1</sup>). The quantity  $P_{\max}$  is related to the integrated intensity  $S$  (in cm<sup>-2</sup>-atmos<sup>-1</sup>) through the relation

$$P_{\max} = S(mc^2/2\pi kT\nu_{lu}^2)^{1/2};$$

the quantity  $S$  (in cm<sup>-2</sup>-atmos<sup>-1</sup>) is related to the dimensionless  $f$  value through the expression

$$S = 2.3789 \times 10^7 (273.1/T) f.$$

It is apparent from Eq. (1) that the dimensionless ratio  $R = A[\nu_{lu}(K)]/R^0(\nu_{lu})(mc^2/2\pi kT\nu_{lu}^2)^{-1}$  is a unique function<sup>2</sup> of  $P_{\max}X$ , i.e.,  $R = \varphi(P_{\max}X)$ . If  $R = R_1$  for  $X = X_1$  and  $R = R_2$  for  $X = X_2$ , then  $R_1/R_2 = \varphi(P_{\max}X_1)/\varphi(P_{\max}X_2) = \varphi^1(P_{\max}X_1, X_1/X_2)$ . The function  $\varphi^1$  can be determined without difficulty for arbitrary values of  $X_1/X_2$ . For  $X_1/X_2 = 2$  the results have been published elsewhere.<sup>1</sup> From the known values of  $X_1/X_2$  and the measured values of  $R_1/R_2$  it is a simple matter to obtain  $P_{\max}X_1$  and hence  $P_{\max}$  or  $S$ . In this manner absolute  $f$  values can be determined from relative intensity measurements for spectral lines with Doppler contour.

For studies in the visible and ultraviolet regions of molecular spectra, and at ordinary temperatures,  $h\nu_{lu} \gg kT$  and<sup>1</sup>

$$\frac{\partial \ln \{P_{\max}(K)X / [g_u(q_{lu})^2] \kappa\}}{\partial (E_u - h\nu_{lu})} = -1/kT, \quad (2)$$

where  $g_u(q_{lu})^2$  represents the relative transition probability for the line with index  $K$ ,  $E_u$  is the energy of the upper state, and  $h$  is Planck's constant. At fixed values of  $T$ , Eq. (2) is useful for checking the consistency of experimentally determined values of  $P_{\max}(K)X$ .

The two-path absorption experiments can be generalized to spectral lines with combined Doppler- and collision-broadening if the line shape is known or is to be measured.

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<sup>1</sup> S. S. Penner, J. Chem. Phys. **20**, 1341 (1952).

<sup>2</sup> R. Ladenburg, Z. Physik **65**, 200 (1930).